

# Entry: Applications

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Economics 567

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Ciliberto and  
Tamer (2009)

Ciliberto and  
Zhang (2017)

Ciliberto,  
Murry, and  
Tamer (2021)

References

- 1 Ciliberto and Tamer (2009)
- 2 Ciliberto and Zhang (2017)
- 3 Ciliberto, Murry, and Tamer (2021)

## Section 1

# Ciliberto and Tamer (2009)

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References

## “Market structure and multiple equilibria in airline markets”

- **Flexible** entry model of airlines
  - Heterogeneity
  - Equilibrium selection
  - ⇒ Partial identification
- Results:
  - Heterogeneity in profit functions
    - Large legacy carriers vs low-cost carriers
    - Airport presence
  - Effect of repealing Wright amendment

# Profits of firm if present in market:

firm-market characteristics

market characteristics

airline

market

$$\pi_{im}(\theta; y_{-im}) = S_m' \alpha_i + Z_{im}' \beta_i + W_{im}' \gamma_i +$$

firm-market characteristics

$$+ \sum_{j \neq i} \underbrace{\left( \delta_j^i y_{jm} + Z_{jm}' \phi_j^i y_{jm} \right)}_{\substack{\text{effect of } j \text{ on } i \\ \text{if firm } j \text{ in } m}} + \epsilon_{im}$$

- Coefficients heterogeneous
- Complete information (all firms know all  $\epsilon_{im}$ )

# Multiple Equilibria

- Simplified 2 player model:

$$y_{1m} = 1 \{ \alpha'_1 X_{1m} + \delta_2^1 y_{2m} + \epsilon_{1m} \geq 0 \}$$

$$y_{2m} = 1 \{ \alpha'_2 X_{2m} + \delta_1^2 y_{1m} + \epsilon_{2m} \geq 0 \}$$

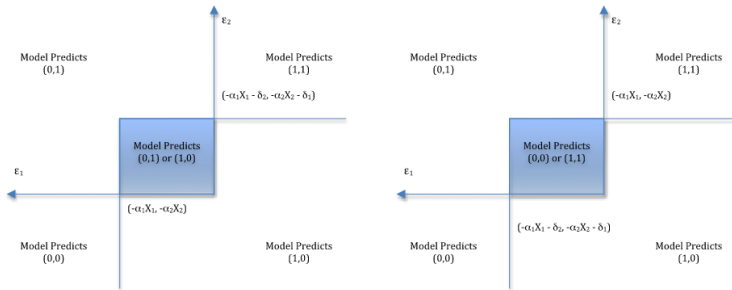


FIGURE 1.—Regions for multiple equilibria: LHP,  $\delta_1, \delta_2 < 0$ ; RHP,  $\delta_1, \delta_2 > 0$ .

# Probability Bounds

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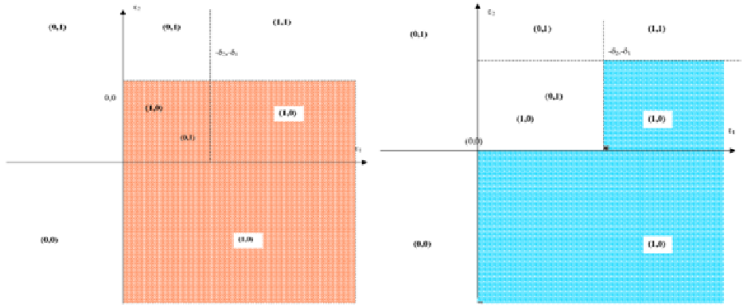


FIGURE 2.—Upper and lower probability bounds on the  $\Pr(1, 0)$ . The shaded area in the graph on the right hand side represents the region for  $(\varepsilon_1, \varepsilon_2)$  that would predict the outcome  $(1, 0)$  uniquely. The shaded region in the graph on the left hand side represents the region where  $(1, 0)$  would be predicted if we *always* select  $(1, 0)$  to be the equilibrium in the region of multiplicity. The probability of the epsilons falling in the respective regions provides an upper and a lower bound on the probability of observing  $(1, 0)$ .

## Estimation

- Model implies conditional moment inequalities

$$H_1(\theta, X) \leq P(y|X) \leq H_2(\theta, X)$$

- Population objective function

$$Q(\theta) = \int \left\| (P(X) - H_1(X, \theta))_- \right\| + \left\| (P(X) - H_2(X, \theta))_+ \right\| dF_X$$

- Sample objective function

$$Q_n(\theta) = \frac{1}{n} \sum_i \left\| (P_n(X_i) - H_1(X_i, \theta))_- \right\| + \left\| (P_n(X_i) - H_2(X_i, \theta))_+ \right\|$$

- Estimate:  $\hat{\Theta} = \{\theta : nQ_n(\theta) \leq \log n\}$



- Second quarter of the 2001 Airline Origin and Destination Survey
- Market = trip between any two of top 100 MSAs
- Airlines: American (AA), Delta (DL), United (UA), SouthWest (WN), medium airlines (MA, includes America West, Continental, Northwest, USAir), low cost carriers (LCC)
- “Cost” = (distance of shortest connecting flight through hub – distance of direct flight) / (distance of direct flight)

TABLE I  
SUMMARY STATISTICS

%	AA	DL	UA	MA	LCC	WN
Airline (%)	0.426 (0.494)	0.551 (0.497)	0.275 (0.447)	0.548 (0.498)	0.162 (0.369)	0.247 (0.431)
Airport presence (%)	0.422 (0.167)	0.540 (0.180)	0.265 (0.153)	0.376 (0.135)	0.098 (0.077)	0.242 (0.176)
Cost (%)	0.736 (1.609)	0.420 (1.322)	0.784 (1.476)	0.229 (0.615)	0.043 (0.174)	0.302 (0.860)
Market level variables						
Wright amendment (0/1)			0.029 (0.169)			
Dallas airport (0/1)			0.070 (0.255)			
Market size (population)			2,258,760 (1,846,149)			
Per capita income (\$)			32,402.29 (3911.667)			
Income growth rate (% * 100)			5.195 (0.566)			
Market distance (miles)			1084.532 (624.289)			
Closest airport (miles)			34.623 (20.502)			
U.S. center distance (miles)			1570.614 (593.798)			
Number of markets			2742			

**TABLE II**  
**DISTRIBUTION OF THE NUMBER OF CARRIERS BY MARKET SIZE<sup>a</sup>**

Number of Firms	Large	Medium	Small	Total
0	7.07	7.31	7.73	7.29
1	41.51	22.86	20.91	30.63
2	29.03	24.30	22.14	25.93
3	12.23	19.67	16.34	15.72
4	8.07	15.14	14.59	11.93
5	1.66	9.58	16.17	7.48
6	0.42	1.13	2.11	1.02
<b>Number</b>	<b>1202</b>	<b>971</b>	<b>569</b>	<b>2742</b>

<sup>a</sup>Cross-tabulation of the percentage of firms serving a market by the market size, which is here measured by the geometric mean of the populations at the market endpoints.

TABLE III  
EMPIRICAL RESULTS<sup>a</sup>

	Berry (1992)	Heterogeneous Interaction	Heterogeneous Control	Firm-to-Firm Interaction
Competitive fixed effect	[-14.151, -10.581]			
AA		[-10.914, -8.822]	[-9.510, -8.460]	
DL		[-10.037, -8.631]	[-9.138, -8.279]	
UA		[-10.101, -4.938]	[-9.951, -5.285]	
MA		[-11.489, -9.414]	[-9.539, -8.713]	
LCC		[-19.623, -14.578]	[-19.385, -13.833]	
WN		[-12.912, -10.969]	[-10.751, -9.29]	
LAR on LAR				
LAR: AA, DL, UA, MA				[-9.086, -8.389]
LAR on LCC				[-20.929, -14.321]
LAR on WN				[-10.294, -9.025]
LCC on LAR				[-22.842, -9.547]
WN on LAR				[-9.093, -7.887]
LCC on WN				[-13.738, -7.848]
WN on LCC				[-15.950, -11.608]
Airport presence	[3.052, 5.087]	[11.262, 14.296]	[10.925, 12.541]	[9.215, 10.436]
Cost	[-0.714, 0.024]	[-1.197, -0.333]	[-1.036, -0.373]	[-1.060, -0.508]
Wright	[-20.526, -8.612]	[-14.738, -12.556]	[-12.211, -10.503]	[-12.092, -10.602]
Dallas	[-6.890, -1.087]	[-1.186, 0.421]	[-1.014, 0.324]	[-0.975, 0.224]
Market size	[0.972, 2.247]	[0.532, 1.245]	[0.372, 0.960]	[0.044, 0.310]
WN			[0.358, 0.958]	
LCC			[0.215, 1.509]	

(Continues)

TABLE III—Continued

	Berry (1992)	Heterogeneous Interaction	Heterogeneous Control	Firm-to-Firm Interaction
Market distance	[4.356, 7.046]	[0.106, 1.002]	[0.062, 0.627]	[−0.057, 0.486]
WN			[−2.441, −1.121]	
LCC			[−0.714, 1.858]	
Close airport	[4.022, 9.831]	[−0.769, 2.070]	[−0.289, 1.363]	[−1.399, −0.196]
WN			[1.751, 3.897]	
LCC			[0.392, 5.351]	
U.S. center distance	[1.452, 3.330]	[−0.932, −0.062]	[−0.275, 0.356]	[−0.606, 0.242]
WN			[−0.357, 0.860]	
LCC			[−1.022, 0.673]	
Per capita income	[0.568, 2.623]	[−0.080, 1.010]	[0.286, 0.829]	[0.272, 1.073]
Income growth rate	[0.370, 1.003]	[0.078, 0.360]	[0.086, 0.331]	[0.094, 0.342]
Constant	[−13.840, −7.796]	[−1.362, 2.431]	[−1.067, −0.191]	[0.381, 2.712]
MA			[−0.016, 0.852]	
LCC			[−2.967, −0.352]	
WN			[−0.448, 1.073]	
Function value	1756.2	1644.1	1627	1658.3
Multiple in identity	0.837	0.951	0.943	0.969
Multiple in number	0	0.523	0.532	0.536
Correctly predicted	0.328	0.326	0.325	0.308

<sup>a</sup> These set estimates contain the set of parameters that cannot be rejected at the 95% confidence level. See Chernozhukov, Hong, and Tamer (2007) and the Supplemental Material for more details on constructing these confidence regions.

VARIABLE COMPETITIVE EFFECTS

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	Independent Unobs	Variance-Covariance	Only Costs
<b>Fixed effect</b>			
AA	[-9.433, -8.485]	[-8.817, -8.212]	[-11.351, -9.686]
DL	[-10.216, -9.255]	[-9.056, -8.643]	[-12.472, -11.085]
UA	[-6.349, -3.723]	[-4.580, -3.813]	[-10.671, -8.386]
MA	[-9.998, -8.770]	[-7.476, -6.922]	[-11.906, -10.423]
LCC	[-28.911, -20.255]	[-14.952, -14.232]	[-11.466, -8.917]
WN	[-9.351, -7.876]	[-6.570, -5.970]	[-12.484, -10.614]
<b>Variable effect</b>			
AA	[-5.792, -4.545]	[-4.675, -3.854]	
DL	[-3.812, -2.757]	[-3.628, -3.030]	
UA	[-10.726, -5.645]	[-8.219, -7.932]	
MA	[-6.861, -4.898]	[-7.639, -6.557]	
LCC	[-9.214, 13.344]		
WN	[-10.319, -8.256]	[-11.345, -10.566]	
Airport presence	[14.578, 16.145]	[10.665, 11.260]	
Cost	[-1.249, -0.501]	[-0.387, -0.119]	
AA			[-0.791, 0.024]
DL			[-1.236, 0.069]
UA			[-1.396, -0.117]
MA			[-1.712, 0.072]
LCC			[-17.786, 1.045]
WN			[-0.802, 0.169]
Wright	[-17.800, -16.346]	[-16.781, -15.357]	[-14.284, -10.479]
Dallas	[0.368, 1.323]	[0.839, 1.132]	[-5.517, -2.095]
Market size	[0.230, 0.535]	[0.953, 1.159]	[1.946, 2.435]
WN	[0.260, 0.612]	[0.823, 1.068]	
LCC	[-0.432, 0.507]		
Market distance	[0.009, 0.645]	[0.316, 0.724]	[-0.039, 1.406]
WN	[-3.091, -1.819]	[-2.036, -1.395]	

TABLE V

MARGINAL EFFECTS<sup>a</sup>Entry:  
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	AA	DL	UA	MA	LCC	WN	No Firms
Market size							
Positive	<i>0.1188</i>	<i>0.1136</i>	<i>0.0571</i>	<i>0.1188</i>	<i>0.0849</i>	<i>0.1118</i>	-0.0033
Negative	-0.0494	-0.0720	-0.0001	-0.0442	<i>-0.1483</i>	-0.0300	-0.0033
Market distance							
Positive	0.0177	0.0165	0.0106	0.0177	0.0099	0.0000	0.0006
Negative	<i>-0.0354</i>	<i>-0.0377</i>	<i>-0.0110</i>	<i>-0.0360</i>	<i>-0.0128</i>	<i>-0.0377</i>	0.0006
Close airport							
Positive	<i>0.1178</i>	<i>0.1122</i>	<i>0.0312</i>	<i>0.1048</i>	0.0662	<i>0.1178</i>	-0.0033
Negative	-0.0375	-0.0518	-0.0004	-0.0318	<i>-0.0911</i>	-0.0175	-0.0033
Change income							
Positive	<i>0.0283</i>	<i>0.0265</i>	<i>0.0149</i>	<i>0.0283</i>	0.0171	<i>0.0277</i>	-0.0007
Negative	-0.0140	-0.0193	-0.0001	-0.0120	<i>-0.0339</i>	-0.0086	-0.0007
Per capita income							
Positive	<i>0.0576</i>	<i>0.0546</i>	<i>0.0291</i>	<i>0.0576</i>	0.0364	<i>0.0573</i>	-0.0015
Negative	-0.0270	-0.0377	-0.0002	-0.0237	<i>-0.0699</i>	-0.0160	-0.0015
U.S. center distance							
Positive	<i>0.0177</i>	<i>0.0181</i>	<i>0.0052</i>	<i>0.0171</i>	0.0038	<i>0.0181</i>	-0.0004
Negative	-0.0044	-0.0055	-0.0001	-0.0033	<i>-0.0076</i>	-0.0011	-0.0004
Airport presence	0.0673	0.0498	0.1888	0.0734	0.0599	0.1040	
Cost	-0.0102	-0.0068	-0.0117	-0.0120	-0.0054	-0.0125	
AA	...	-0.3606	-0.2556	-0.4108	-0.0704	-0.2143	
DL	-0.3336	...	-0.2658	-0.3908	-0.0335	-0.2126	
UA	-0.2486	-0.2630	...	-0.2696	-0.0675	-0.2015	
MA	-0.3877	-0.3941	-0.2717	...	-0.0989	-0.2766	
LCC	-0.0998	-0.1579	-0.0721	-0.1415	...	-0.0411	

TABLE VI  
VARIANCE–COVARIANCE MATRIX

	AA	DL	UA	MA	LCC	WN
AA	1	[0.043, 0.761]	[−0.110, 0.442]	[0.103, 0.626]	[−0.217, 0.752]	[0.055, 0.355]
DL		[5.052, 6.895]	[−0.200, 0.190]	[0.629, 0.949]	[−0.128, 0.656]	[0.218, 0.834]
UA			[2.048, 3.340]	[−0.173, 0.309]	[−0.213, 0.652]	[0.192, 0.797]
MA				[2.396, 5.558]	[−0.094, 0.313]	[0.093, 0.862]
LCC					[2.026, 6.705]	[0.093, 0.764]
WN						[2.063, 2.331]



TABLE VII

PREDICTED PROBABILITIES FOR POLICY ANALYSIS: MARKETS OUT OF DALLAS LOVE

Airline	Variance–Covariance	Independent Obs	Only Costs
No firms	[−0.6514, −0.6384, −0.6215]	[−0.7362, −0.6862, −0.6741]	[−0.6281, −0.6162, −0.5713]
AA	[0.4448, 0.4634, 0.4711]	[0.2067, 0.3013, 0.3280]	[0.3129, 0.3782, 0.4095]
DL	[[0.4768, 0.4988, 0.5056]	0.2733, 0.3774, 0.4033]	[0.3843, 0.4315, 0.4499]
UA	[0.1377, 0.1467, 0.1519]	[0.1061, 0.1218, 0.2095]	[0.2537, 0.3315, 0.3753]
MA	[0.4768, 0.4988, 0.5056]	[0.2733, 0.3774, 0.4033]	[0.3656, 0.4143, 0.4342]
LCC	[0.3590, 0.3848, 0.4156]	[0.8369, 0.8453, 0.8700]	[0.2839, 0.3771, 0.3933]
WN	[0.4480, 0.4744, 0.4847]	[0.2482, 0.2697, 0.3367]	[0.3726, 0.4228, 0.4431]

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References



# Conclusions

## Section 2

# Ciliberto and Zhang (2017)

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References

# “Multiple Equilibria and Deterrence in Airline Markets”

## Section 3

# Ciliberto, Murry, and Tamer (2021)

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